

1. Solve the following initial value problems:

a.  $\frac{dy}{dz} = 5 - \frac{y}{z}$ ;  $y(1)=3$ .

b.  $y' = (y^2/x^2) + (y/x)$ ;  $y(1) = 1$

c.  $y'' - y = 2 e^t$ ;  $y(0)=0$ ;  $y'(0)=3$ .

2. Find general solutions to the following:

a.  $y'' + 4y' + 3y = 16 e^t$

b.  $9y'' + 6y' + y = \frac{1}{4} t^2 - 14$

3. I accidentally left a sheet pan in the oven overnight at  $400^\circ$ . When I removed the pan in the morning it was completely heated to  $400^\circ$ . Ten minutes later it had cooled to  $232^\circ$ . I keep my house at  $64^\circ$ . How "hot" would the pan have been  $t$  minutes after I removed it from the oven? How about an hour after it came out of the oven? (Assume Newton's Law of Cooling applies).